# High-Pressure $\mathbf{M n P}_{4}$, a Polyphosphide with Mn-Mn Pairs 

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#### Abstract

The new compound $\mathrm{MnP}_{4}$ was prepared by reaction of the elemental components at pressures of 30-55 kbar in a tetrahedral anvil high-pressure device. It is a diamagnetic semiconductor with an activation energy of $0 \cdot 14 \mathrm{eV}$ and crystallizes with space group $C 2 / c, a=10 \cdot 513$ (1), $b=5 \cdot 0944$ (4), $c=21 \cdot 804$ (2) $\AA$, $\beta=94.71(1)^{\circ}$, and $Z=16$. The structure was determined from single-crystal counter data by Patterson and Fourier methods and refined to a conventional $R$ of 0.051 for 1765 reflections. The Mn atoms are in octahedral P coordination, and the P atoms are tetrahedrally coordinated by Mn and P atoms. The Mn atoms have formal oxidation number $2+\left(d^{5}\right.$ configuration). Four $\mathrm{MnP}_{6}$ octahedra share edges to form a linear array of four Mn atoms. The Mn atoms are displaced from the centers of the octahedra toward one another to form pairs with a resulting Mn-Mn bonding distance of $2.941 \AA$, thus accounting for the diamagnetism. Average $\mathrm{Mn}-\mathrm{P}$ and $\mathrm{P}-\mathrm{P}$ distances are 2.282 and $2 \cdot 225 \AA$, respectively. $\mathrm{MnP}_{4}$ can be described as an eight-layer stacking variant of the two-layer $\mathrm{CrP}_{4}$ structure, although bonding within and between the layers is of equal strength. Qualitative MO bonding models for the $\mathrm{MnP}_{4}$ and $\mathrm{CrP}_{4}$ structures are presented that allow rationalization of magnetic and conductive properties. A similar bonding proposal is made for the marcasite and arsenopyrite structures which, as is the case for $\mathrm{CrP}_{4}$ and $\mathrm{MnP}_{4}$, have $\mathrm{TP}_{6}$ octahedra linked via edges, with transition metal atoms forming infinite strings and pairs, respectively.


## Introduction

Investigations of the $\mathrm{Mn}-\mathrm{P}$ system at ambient pressure resulted in the characterization of $\mathrm{Mn}_{3} \mathrm{P}, \mathrm{Mn}_{2} \mathrm{P}$, and MnP (Årstad \& Nowotny, 1937; Rundqvist, 1962). Between MnP and P, only the phase $\mathrm{MnP}_{3}$ was found by Biltz, Wiechmann \& Meisel (1937). Its structure is still not known. Recently we reported on the highpressure synthesis, properties, and crystal structure of $\mathrm{CrP}_{4}$ (Jeitschko \& Donohue, 1972) and $\mathrm{CrP}_{2}$ (Jeitschko \& Donohue, 1973). We have now prepared at high pressure and characterized $\mathrm{MnP}_{4}$, which forms $\mathrm{Mn}-\mathrm{Mn}$ pairs. It is related to $\mathrm{CrP}_{4}$ where the Cr atoms form continuous chains.

## Preparation and properties

$\mathrm{MnP}_{4}$ was prepared in a tetrahedral anvil press in a manner similar to that which we reported for $\mathrm{CrP}_{4}$. High-purity ( $>99.9 \%$ ) powders of Mn and red P, mixed in atomic ratios varying between $1: 3$ and $1: 4$, were subjected to temperatures of $1500-1700 \mathrm{~K}$ at pressures of $30-55 \mathrm{kbar}$. After 1-2 hat these conditions the samples were cooled over 1-2 h to 1300 K and quenched while still under pressure. Owing to a temperature gradient along the cylindrical pellet, black crystals grew at the ends of the container. Chemical analysis indicated the formula $\mathrm{MnP}_{4}$. The center of the pellet gave X-ray powder patterns of $\mathrm{MnP}_{4}$ plus diffraction lines of unidentified phases.

Electrical resistivity measurements with the four-

[^0]probe technique on a crystal of unknown orientation showed semiconductor behavior with a room temperature resistivity of 30 ohm cm and an activation energy (from $\varrho=\varrho_{o} \cdot e \exp E_{a} / k T$ ) of 0.14 eV . Magnetic measurements indicated diamagnetism.

## Structure determination

## Unit cell and space group

Single crystals of $\mathrm{MnP}_{4}$, isolated from the quenched and crushed high-pressure samples, were investigated in a Buerger precession camera with Mo K $\alpha$ radiation. They show $2 / m$ symmetry. Diffraction extinctions ( $h k l$ present only with $h+k=2 n ; h 0 l$ only with $l=2 n$ ) are characteristic of space groups $C 2 / c$ and $C c$, of which $C 2 / c$ was found to be correct during the structure determination.
A Guinier-Hägg powder photograph (Table 1), recorded at 298 K with $\mathrm{Cu} K \alpha_{1}$ radiation and highpurity $\mathrm{KCl}(a=6.2931 \AA)$ as standard, was evaluated with a David-Mann film reader and indexed with the unit cell found from the single-crystal photographs. Least-squares refined lattice constants are: $a=$ 10.513 (1), $b=5.0944$ (4), $c=21.804$ (2) $\AA, \beta=94.71$ (1) ${ }^{\circ}$, $V=1163 \cdot 8$ (1) $\AA^{3}$. With the exact composition $\mathrm{MnP}_{4}$ and 16 formula units per cell found during the structure determination, the calculated density is $4.082 \mathrm{~g} \mathrm{~cm}^{-3}$, which compares well with the density of $4.09 \mathrm{~g} \mathrm{~cm}^{-3}$, determined by displacement in bromoform.

## Intensity data

The single crystal selected for the collection of the intensity data had irregular shape with overall exten-
sions varying between 42 and $65 \mu \mathrm{~m}$. Zr -filtered Mo radiation was used with a four-circle automated diffractometer, scintillation counter, and pulse-height discriminator. Scans were over $1 \cdot 0^{\circ}$ in $2 \theta$ plus the angular separation of the $K \alpha$ doublet, with scan speed of $0.4^{\circ}$ $2 \theta \min ^{-1}$. Background was counted for 20 s at both ends of each scan. The intensity of a strong standard reflection varied $\pm 2.0 \%$ over the period of data collection. All reflections within the asymmetric quadrant up to $75^{\circ} 2 \theta$ were measured. The usual Lorentz-polarization correction was applied. No absorption correction was made, since transmission values calculated for

Table 1. Evaluation of a Guinier-Hägg powder pattern of $\mathrm{MnP}_{4}$
$\mathrm{Cu} K \alpha_{1}$ radiation; calculated data were generated by a computer program (Yvon, Jeitschko \& Parthé, 1969) from the refined structure.

the extremes in crystal shape varied only between 74 and $83 \%$. They correspond to relative errors of less than $\pm 2 \cdot 5 \%$ in structure factors.

## Solution and refinement of the structure

The Patterson synthesis, computed with a program by Fritchie \& Guggenberger (1967), showed maxima at $z \approx 0, \frac{1}{8}, \frac{2}{8}, \frac{3}{8}$, etc. Thus it was concluded that the structure contains layers separated from each other by approximately $\Delta z=\frac{1}{8}$. The correspondence of the cell dimensions $a$ and $b$ of $\mathrm{CrP}_{4}$ (Jeitschko \& Donohue, 1972) with $b$ and $a$ of $\mathrm{MnP}_{4}$ was noted, and the similarity (but not equivalence) of the Patterson functions of $\mathrm{CrP}_{4}$ and $\mathrm{MnP}_{4}$ at $z \approx 0$ suggested a close relationship between the two structures. Of further help was our expectation that the Mn atoms would form pairs. With the aid of models it was found that there are two basically different ways of connecting adjacent $\mathrm{CrP}_{4}$-like layers. One mode of linking is compatible with short or long metal-metal interactions and the other does not allow for metal-metal bonds. The correct structure, which was arrived at by trial and error using both possible space groups and successive least-squares refinements of partial structures and difference Fourier syntheses, combines all three kinds of interfaces between adjacent layers.
The structure was refined with a full-matrix leastsquares program by Finger (1969). The sum $\sum w_{i}\left(K F_{o}-\right.$ $\left.\left|F_{c}\right|\right)^{2}$ was minimized, where $w_{i}$ is the weight based on counting statistics, and $K$ the scale factor. Atomic scattering values for neutral atoms were taken from Cromer \& Mann (1968), corrected for anomalous dispersion (Cromer \& Liberman, 1970). Zachariasen's (1963) correction for secondary extinction was used. Structure factors for which this correction amounted to more than $10 \%$, as well as structure factors which were smaller than three times their standard deviations, were given zero weight. Final conventional $R$ values for the refinement with isotropic thermal parameters are 0.056 for 1765 reflections with nonzero weight and 0.112 for the total of 3036 reflections. For the refinement with anisotropic thermal parameters, the corresponding $R$ values are 0.051 and $0 \cdot 109$. Parameters obtained in this

Table 2. Positional and thermal parameters of $\mathrm{MnP}_{4}$
All atoms are in the general position of $C 2 / c$. Numbers in parentheses are e.s.d.'s in the least significant digits. Vibrational parameters ( $\times 10^{5}$ ) are defined through $T=\exp \left(-\sum \sum h_{i} h_{j} \beta_{l}\right)$. The last column contains equivalent isotropic $B$ values. They agree (within their standard deviations) with the values obtained in the least-squares refinement with isotropic thermal parameters.

|  | $x$ | $y$ | $z$ | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12}$ | $\beta_{13}$ | $\beta_{23}$ | $B\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Mn}(1)$ | 0.92576 (9) | $0 \cdot 1172$ (2) | 0.07002 (4) | 62 (6) | 227 (31) | 10 (1) | -24 (11) | -5 (2) | 2 (5) | $0 \cdot 23$ (1) |
| P (1) | $0 \cdot 57712$ (16) | $0 \cdot 3274$ (3) | 0.03698 (7) | 116 (12) | 200 (53) | 13 (3) | 36 (19) | -9 (4) | -7 (9) | $0 \cdot 33$ (2) |
| P (2) | 0.76977 (16) | $0 \cdot 4090$ (3) | 0.08340 (7) | 90 (11) | 296 (51) | 16 (3) | -13 (19) | -16 (4) | 21 (9) | $0 \cdot 34$ (2) |
| $\mathrm{P}(3)$ | 0.07973 (16) | $0 \cdot 4207$ (3) | 0.07441 (7) | 126 (11) | 137 (50) | 14 (3) | - 15 (19) | -5 (4) | 0 (9) | $0 \cdot 32$ (2) |
| $\mathrm{P}(4)$ | 0.77567 (16) | 0.8099 (3) | 0.04916 (7) | 105 (12) | 262 (52) | 11 (3) | -17 (19) | -7 (4) | 4 (9) | $0 \cdot 32$ (2) |
| $\mathrm{Mn}(2)$ | 0.31551 (9) | $0 \cdot 8018$ (2) | $0 \cdot 18209$ (4) | 60 (7) | 256 (30) | 8 (1) | -26 (11) | -7 (2) | 2 (5) | $0 \cdot 23$ (1) |
| P (5) | $0 \cdot 47458$ (15) | $0 \cdot 5175$ (3) | $0 \cdot 17056$ (7) | 87 (11) | 203 (49) | 17 (3) | 30 (19) | -3 (4) | 7 (9) | $0 \cdot 31$ (2) |
| $\mathrm{P}(6)$ | $0 \cdot 17128$ (16) | $0 \cdot 1223$ (3) | 0.21538 (7) | 83 (11) | 239 (49) | 22 (3) | 35 (20) | -11 (4) | 4 (9) | $0 \cdot 35$ (2) |
| $\mathrm{P}(7)$ | $0 \cdot 16026$ (16) | $0 \cdot 5081$ (3) | $0 \cdot 16917$ (8) | 92 (11) | 356 (52) | 13 (3) | -31(19) | -3 (4) | -9 (9) | $0 \cdot 35$ (2) |
| $\mathbf{P}(8)$ | $0 \cdot 46793$ (16) | $0 \cdot 1058$ (3) | $0 \cdot 19999$ (7) | 103 (11) | 288 (52) | 16 (2) | 63 (20) | -5 (4) | 6 (9) | $0 \cdot 36$ (2) |

refinement* are listed in Table 2. Within their standard deviations, positional parameters are the same in the refinements with isotropic and anisotropic thermal parameters. The ratio of the long to the short axis of the thermal ellipsoids varies between $1 \cdot 35[\mathrm{Mn}(1)]$ and $2 \cdot 6[\mathrm{P}(2)]$. These ellipsoids are somewhat affected by errors in the data due to absorption. The low $R$ values

* A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 30692 (17 pp., 1 microfiche). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1 NZ, England.
of 0.044 (isotropic) and 0.039 (anisotropic thermal parameters) for the 1366 strongest reflections indicate better the accuracy of the structure determination than the overall $R$ values given above, which are strongly affected by the large number of weak reflections with poor counting statistics.


## Description of the structure and comparison with $\mathbf{C r P}_{\mathbf{4}}$

The crystal structure of $\mathrm{MnP}_{4}$ is best described as a layer structure although bonding within and between the layers is of equal strength. The layers are all of the same kind (disregarding slight differences in bond




- Mn2


Fig. 1. Normal projections of the $\mathrm{MnP}_{4}$ structure. On the right-hand side the atomic layers at $z \sim \frac{15}{15}, \frac{1}{16}, \frac{3}{16}$, etc., are shown from the side. Each layer contains either $\mathrm{Mn}(1)$ or $\mathrm{Mn}(2)$ atoms. The three types of interfaces between adjacent layers are shown on the left-hand side. They allow for $\mathrm{Mn}(1)-\mathrm{Mn}(1), \mathrm{Mn}(1)-\mathrm{Mn}(2)$, and $\mathrm{Mn}(2)-\mathrm{Mn}(2)$ interactions. Only the interaction $\mathrm{Mn}(1)-$ $\mathrm{Mn}(2)$ is bonding. In spite of the appearance in the projections, the $\mathrm{P}_{6}$ octahedra around $\mathrm{Mn}(2)$ atoms of adjacent layers (e.g at $z \sim \frac{3}{16}$ and $\frac{5}{16}$ ) do not share edges but corners.
distances and angles) with one Mn and four P atoms forming a puckered tessellation of pentagons and hexagons. The layers at $z \sim \frac{15}{16}$ and $\frac{1}{16}$ (Fig. 1) correspond to the two-layer structure of $\mathrm{CrP}_{4}$ (Jeitschko \& Donohue, 1972). In $\mathrm{MnP}_{4}$ eight layers of different orientation and connectivity are needed to complete one unit cell. The four subsequent layers at $z \sim \frac{13}{16}, \frac{15}{16}$, $\frac{1}{16}$, and $\frac{3}{16}$ are parallel to each other. The subsequent four layers at $z \sim \frac{5}{16}, \frac{7}{16}, \frac{9}{16}$, and $\frac{11}{16}$ are also parallel to each other, but, relative to the adjacent layers above and below, rotated $180^{\circ}$ around an axis perpendicular to the layers. This can best be seen by comparing the inclination of $\mathrm{MnP}_{6}$ octahedra of adjacent layers (Fig. 2).

The two independent Mn atoms are in approximately octahedral coordination to P atoms. The Mn atoms of four adjacent parallel layers together with their $P$ neighbors form a group of four edge-sharing $\mathrm{MnP}_{6}$ octahedra, which are connected to other $\mathrm{MnP}_{6}$ octahedra above and below by corners. Within the group of four edge-sharing $\mathrm{MnP}_{6}$ octahedra there are two short $\mathrm{Mn}(1)-\mathrm{Mn}(2)$ interactions (Fig. 3). Bonding distances Mn-P vary from $2 \cdot 215$ to $2.380 \AA$ with average distances of $2.278 \AA$ for $\mathrm{Mn}(1)$ and $2.286 \AA$ for $\mathrm{Mn}(2)$. Those $\mathrm{P}-\mathrm{Mn}-\mathrm{P}$ angles which in a regular octahedron are $90^{\circ}$, vary between 74 and $99^{\circ}$.

The eight independent $P$ atoms are all in more or less distorted tetrahedral coordination. $\mathrm{P}(1), \mathrm{P}(2), \mathrm{P}(5)$, and $P(6)$ are coordinated to 2 Mn and 2 P atoms. The other four P atoms each have 1 Mn neighbor and 3 P neighbors. Tetrahedral bond angles $\mathrm{Mn}-\mathrm{P}-\mathrm{P}$ and


Fig. 3. Near-neighbor environments of the Mn atoms in $\mathrm{MnP}_{4}$.


Fig. 2. Stereo drawing of the $\mathrm{MnP}_{4}$ structure. The Mn atoms are drawn as large spheres.

P-P-P vary from 94 to $130^{\circ}$ and from 89 to $106^{\circ}$, respectively. The four different $\mathrm{Mn}-\mathrm{P}-\mathrm{Mn}$ angles are shown in Fig. 3. P-P distances cover the range from $2 \cdot 177$ to $2 \cdot 278 \AA$. The average P-P distance of $2 \cdot 225 \AA$ agrees well with the average P-P distances of $2.21 \pm$ $0.02 \AA$ in elemental $P$ modifications (Brown \& Rundqvist, 1965; Thurn \& Krebs, 1969), in $\mathrm{CdP}_{4}$ (Krebs, Müller \& Zürn, 1956), in $\mathrm{TlP}_{5}$ (Olofsson \& Gullmann, 1971), and in alkali and earth alkali polyphosphides as $\mathrm{Na}_{3} \mathrm{P}_{11}$ (Wichelhaus \& von Schnering, 1973), $\mathrm{Sr}_{3} \mathrm{P}_{14}$ (Dahlmann \& von Schnering, 1972), and $\mathrm{SrP}_{3}$ (Dahlmann \& von Schnering, 1973).

The average P-P distance of $2 \cdot 213 \AA$ in $\mathrm{CrP}_{4}$ is slightly smaller than the average P-P distance of $2 \cdot 225 \AA$ in $\mathrm{MnP}_{4}$. This is probably due to larger deviations from ideal P-P bonding distances in $\mathrm{MnP}_{4}$.* Average isotropic thermal parameters in $\mathrm{CrP}_{4}$ and $\mathrm{MnP}_{4}$ are very similar with 0.27 and $0.35 \AA^{2}$ for Cr and P in $\mathrm{CrP}_{4}$, and 0.23 and $0.34 \AA^{2}$ for Mn and P in $\mathrm{MnP}_{4}$. Systematic errors in these values, due to systematic differences in the absorption of low- and high-angle reflections (which were not corrected for), were calculated to be less than $0.01 \AA^{2}$.

The rationalization of the $\mathrm{MnP}_{4}$ and $\mathrm{CrP}_{4}$ structures as stacking variants of one net, allows one to predict structures with other stacking sequences for binary and

[^1]Table 3. Interatomic distances in $\mathrm{MnP}_{4}(\AA)$
Standard deviations, computed from e.s.d.'s of positional parameters and lattice constants, are all less than $0.003 \AA$. All distances shorter than $3.6 \AA$ (for Mn ) and $2.8 \AA$ (for P atoms) are listed.

| $\mathrm{Mn}(1)-\mathrm{P}(1)$ | 2.326 | $\mathrm{Mn}(2)-\mathrm{P}(2)$ | 2.234 |
| :---: | :---: | :---: | :---: |
| $-\mathrm{P}(1)$ | 2.347 | $-\mathrm{P}(5)$ | 2.241 |
| $-\mathrm{P}(2)$ | 2.249 | $-\mathrm{P}(6)$ | 2.380 |
| $-\mathrm{P}(3)$ | 2.235 | $-\mathrm{P}(6)$ | 2.409 |
| $-\mathrm{P}(4)$ | 2.243 | $-\mathrm{P}(7)$ | 2.215 |
| $-\mathrm{P}(5)$ | 2.268 | $-\mathrm{P}(8)$ | 2.240 |
| $-\mathrm{Mn}(2)$ | 2.941 | $-\mathrm{Mn}(1)$ | 2.941 |
| $\mathrm{P}(1)-\mathrm{Mn}(1)$ | 2.326 | $\mathrm{P}(5)-\mathrm{Mn}(1)$ | 2.268 |
| $-\mathrm{Mn}(1)$ | 2.347 | $-\mathrm{Mn}(2)$ | 2.241 |
| $-\mathrm{P}(2)$ | 2.229 | $-\mathrm{P}(6)$ | 2.278 |
| $-\mathrm{P}(3)$ | 2.26 | $-\mathrm{P}(8)$ | 2.196 |
| $\mathrm{P}(2)-\mathrm{Mn}(1)$ | 2.249 | $\mathrm{P}(6)-\mathrm{Mn}(2)$ | 2.380 |
| $-\mathrm{Mn}(2)$ | 2.234 | $-\mathrm{Mn}(2)$ | 2.409 |
| $-\mathrm{P}(1)$ | 2.229 | $-\mathrm{P}(5)$ | 2.278 |
| $-\mathrm{P}(4)$ | 2.177 | $-\mathrm{P}(7)$ | 2.207 |
| $\mathrm{P}(3)-\mathrm{Mn}(1)$ | 2.235 | $\mathrm{P}(7)-\mathrm{Mn}(2)$ | 2.215 |
| $-\mathrm{P}(1)$ | 2.226 | $-\mathrm{P}(3)$ | 2.214 |
| $-\mathrm{P}(4)$ | 2.246 | $-\mathrm{P}(6)$ | 2.207 |
| $-\mathrm{P}(7)$ | 2.214 | $-\mathrm{P}(8)$ | 2.237 |
| $\mathrm{P}(4)-\mathrm{Mn}(1)$ | 2.243 | $\mathrm{P}(8)-\mathrm{Mn}(2)$ | 2.240 |
| $-\mathrm{P}(2)$ | 2.177 | $-\mathrm{P}(5)$ | 2.196 |
| $-\mathrm{P}(3)$ | 2.246 |  | $-\mathrm{P}(7)$ |
| $-\mathrm{P}(4)$ | 2.252 |  | 2.237 |
|  |  | $\mathrm{P}(8)$ | 2.230 |

ternary compounds $\mathrm{TX}_{4}$, depending on the bonding requirements of the transition metal ( T ) and metalloid (X) atoms, as is known for compositions $\mathrm{TX}_{2}$ with pyrite, marcasite, $\mathrm{PdP}_{2}, \mathrm{PdS}_{2}, \mathrm{PdPS}$, and $\mathrm{AuSn}_{2}$ ( $\alpha$ - $\mathrm{NiAs}_{2}$ ) type structures (Jeitschko, 1974).

## Bonding in $\mathbf{M n P}_{\mathbf{4}}$ and $\mathbf{C r P}_{4}$

In a qualitative valence-bond description $s p^{3}$ and $d^{2} s p^{3}$ hybridization can be assumed for the P and Mn atoms, respectively. Ascribing two electrons to each of the short $\mathrm{Mn}-\mathrm{P}$ and $\mathrm{P}-\mathrm{P}$ interactions, the Mn atoms obtain a $d^{5}$ system (oxidation number $2+$ ). The same result is arrived at by assigning oxidation number zero to each P atom bonded to 3 P and 1 Mn , and oxidation number 1 - to each P bonded to 2 P and 2 Mn atoms. Two nonbonding electrons can be accommodated in each of two $t_{2 g}$ orbitals while the fifth electron occupies the third $t_{2 g}$ orbital and forms a bond with the corresponding electron of one neighboring Mn atom. This results in the formation of $\mathrm{Mn}(1)-\mathrm{Mn}(2)$ pairs in agreement with the diamagnetic behavior of the compound.

The $\mathrm{Mn}(1)-\mathrm{Mn}(2)$ distance of $2.94 \AA$ is rather long for a bonding distance when compared to the 'normal' single-bond distance of $2.4 \AA$, but the distortions in bond angles (tetrahedral angles are reduced from 109 to 81 and $82^{\circ}$, octahedral angles are widened from 90 to 98 and $99^{\circ}$ ) clearly indicate the bonding $\mathrm{Mn}(1)-\mathrm{Mn}(2)$ interaction (Fig. 3). If the electrons in the $\mathrm{Mn}-\mathrm{P}$ bonds are counted as one belonging to Mn and the other one to P , the Mn atoms obtain a formal charge of $4-$. Although the actual charge distribution is not known, electrostatic repulsion may also contribute to the stretching of the $\mathrm{Mn}(1)-\mathrm{Mn}(2)$ bond. The latter argument was used to explain the unexpected length of the $\mathrm{Mn}-\mathrm{Mn}$ bond of $2.92 \AA$ in $\mathrm{Mn}_{2}(\mathrm{CO})_{10}$ (Dahl \& Rundle, 1963). There, of course, the bonding $\mathrm{Mn}-\mathrm{Mn}$ interaction is indisputable, since there are no other bonds between the Mn atoms. For the same reason no superexchange mechanism is possible, and by analogy, does not need to be invoked for $\mathrm{MnP}_{4}$. Metal-metal bonding, indicated by distortions of near-neighbor environments, occurs for distances as long as $3 \cdot 31 \AA$, as was found in $\mathrm{NbI}_{4}$ (Dahl \& Wampler, 1962). The fact that the $\mathrm{MnP}_{6}$ octahedra are linked by edges is additional evidence for $\mathrm{Mn}-\mathrm{Mn}$ bonding, since linking by corners is favoured for electrostatic reasons, as long as the $\mathrm{Mn}-\mathrm{P}$ bonds have some polarity. Corner-sharing is geometrically possible, as demonstrated by $\mathrm{CdP}_{4}$ and it occurs even for compositions with lower metalloid $(\mathrm{X})$ content as in the large number of compounds with skutterudite ( $\mathrm{TX}_{3}$ ) and pyrite ( $\mathrm{TX}_{2}$ ) type structure.

Near-neighbor distortions and diamagnetism or Pauli paramagnetism* also indicated metal-metal

[^2]bonding in $\mathrm{CrP}_{4}$, where $\mathrm{Cr}^{2+}$ with low spin $d^{4}$ configuration is also in octahedral $\mathbf{P}$ environment and the $\mathrm{CrP}_{6}$ octahedra share edges to form zigzag chains with $\mathrm{Cr}-\mathrm{Cr}$ bonding distances of $3 \cdot 18 \AA$ (Jeitschko \& Donohue, 1972). There, as in $\mathrm{MnP}_{4}$, the optimization of all bonding interactions seems not possible for geometric reasons.*

A comparison of the $\mathrm{MnP}_{4}$ structure with the structure of $\mathrm{CrP}_{4}$ allows one to rationalize why $\mathrm{CrP}_{4}$ is a metal, while $\mathrm{MnP}_{4}$ is a semiconductor. In accordance with bonding descriptions given by Bither, Bouchard, Cloud, Donohue \& Siemons (1968) for TX 2 compounds ( $\mathrm{T}=$ transition metal, $\mathrm{X}=\mathrm{S}, \mathrm{Se}, \mathrm{Te}$ ) with pyrite structure, we assume the $d$ levels of the metal atoms in $\mathrm{MnP}_{4}$ and $\mathrm{CrP}_{4}$ to be located between the bonding and antibonding T-P and P-P bonds (Fig. 4). The relatively long $\mathrm{Cr}-\mathrm{Cr}$ distances of $3.18 \AA$ in $\mathrm{CrP}_{4}$ allow only weak bonding and band splitting. Consequently the bonding and antibonding $\mathrm{Cr}-\mathrm{Cr} d$ functions overlap, giving rise to metallic conductivity. In $\mathrm{MnP}_{4}$ the $\mathrm{Mn}-\mathrm{Mn}$ bond is shorter ( $2 \cdot 94 \AA$ ). This results in stronger $\mathrm{Mn}-\mathrm{Mn}$ bonds and larger splitting of bonding and antibonding $d$ bands. If the splitting is large enough a band gap develops as shown in Fig. 4; however, even if those bands are not completely separated in energy, $\mathrm{MnP}_{4}$ could be semiconducting simply because the $\mathrm{Mn}-\mathrm{Mn}$ interactions are not continuous throughout the structure.

The kind of metal-metal bonding in $\mathrm{CrP}_{4}$ with continuous zigzag chains of edge-sharing octahedra is also found in $\beta-\mathrm{ReO}_{2}$ (Magnéli, 1957). Pairing of metal atoms across edges of edge-sharing octahedra as found in $\mathrm{MnP}_{4}$ also occurs in several transition-metal oxides and halides, e.g. $\mathrm{NbO}_{2}$ and $\mathrm{NbCl}_{4}$ (Schäfer \& von Schnering, 1964). In all these compounds, it is generally agreed that the short metal-metal distances represent bonding metal-metal interactions. Thus metal-metal pairs are formed by single bonds in $\mathrm{NbO}_{2}$ and by double bonds in $\mathrm{MoO}_{2}$ (Rogers, Shannon, Sleight \& Gillson, 1969).

[^3]
## Marcasites and arsenopyrites

The short metal-metal distances in $\mathrm{CrP}_{4}$ and $\mathrm{MnP}_{4}$ have their counterparts in the large number of compositions $\mathrm{TX}_{2}$ with arsenopyrite and loellingite structure (Hulliger, 1968) where the short metal-metal distances also occur across edges of edge-sharing octahedra. In the arsenopyrites (where the metal atoms have a $d^{5}$ configuration), pairing of the metal atom occurs, as is the case for the Mn atoms in $\mathrm{MnP}_{4}$ which also have $d^{5}$ configuration. In the loellingites (=marcasites with the T atoms in $d^{2}$ and $d^{4}$ configuration) the metal atoms form continuous straight strings, while continuous zigzag chains are formed for Cr atoms ( $d^{4}$ ) in $\mathrm{CrP}_{4}$.
Several conflicting bonding models have been suggested for the arsenopyrites and marcasites. A detailed review of these models will not be given here and the reader is referred to the original papers (Hulliger \& Mooser, 1965; Pearson, 1965; Brostigen \& Kjekshus, 1970; Goodenough, 1972). It is, however, remarkable that not one of the more recent bonding models allows for metal-metal bonding in the loellingites, quite in contrast with the generally accepted view that short interatomic distances indicate bonding, especially when alternate structures are competing (as is the pyrite structure in this case), where the short nonbonding interactions could be avoided.
We therefore propose yet another model which has $\sigma$ and $\pi$ metal-metal bonding in the $d^{2}$ and $d^{4}$ marcasites and $\sigma$ metal-metal bonds in the ( $d^{5}$ ) arsenopyrites. It requires the usual mixing of the $d_{x 2-y 2}, d_{22}, s$, and $p^{3}$ states to form $\sigma$ bonds to the octahedrally surrounding X atoms. The (say) $d_{x y}$ orbital is then $\sigma$ bonding with the neighboring metal atoms. A linear combination of the remaining $d_{x z}$ and $d_{y z}$ orbitals results in one orbital which is nonbonding with respect to metal neighbors and one orbital which is $\pi$ bonding with the corresponding orbitals of the neighboring metal atoms. In this way each T atom forms two $\sigma$ and two $\pi \mathrm{T}$-T half-bonds in the $d^{2}$ and $d^{4}$ marcasites, thus accounting for the short $c$ axis in these marcasites. In the arsenopyrites the metal atoms have $d^{5}$ configuration and only one ( $\sigma$ ) metal-metal bond can be formed per T atom, resulting in T-T pairing. For the $d^{6}$ marcasites no



Fig. 4. Schematic MO energy-level diagrams for $\mathrm{CrP}_{4}$ and $\mathrm{MnP}_{4}$. Numbers in brackets refer to states per formula unit.
metal-metal bonding exists as was also assumed in previous bonding proposals, and the $c$ axis is therefore greater in the $d^{6}$ marcasites than in the $d^{4}$ marcasites. ${ }^{*}$

The present model differs from the one proposed by Goodenough (1972) mainly in the relative position of bonding and nonbonding $t_{2 g}$ levels above and below the Fermi level. Thus conductive and magnetic properties are similar for both models and our model agrees well with the experimental findings for $\mathrm{FeAs}_{2}, \mathrm{FeSb}_{2}$ (Fan, Rosenthal, McKinzie \& Wold, 1972), and $\mathrm{FeAs}_{2-x} \mathrm{Se}_{x}$ (Baghdadi \& Wold, 1974).

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* Table I of the paper by Brostigen \& Kjekshus (1970) lists a $d^{0}$ defect marcasite $\mathrm{Mo}_{2 / 3} \mathrm{As}_{2}$ with short $c$ axis. This compound seems to contradict our bonding proposal [but might be considered as supporting Goodenough's (1972) model] since a long $c$ axis would be expected for a $d^{\circ}$ compound where no T-T bonds are possible. However, bonding in a defect structure is certainly quite different from that in a compound with stoichiometry $\mathrm{TX}_{2}$. Furthermore, this compound, reported with composition $\mathrm{Mo}_{0.4} \mathrm{As}_{2}$ by Brown (1965), could not be confirmed in subsequent investigations of the Mo-As system by Taylor, Calvert \& Hunt (1965) and Jensen, Kjekshus \& Skansen (1966).


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[^0]:    * Contribution No. 2180.

[^1]:    * In a solid-state compound generally not all bonding distances can be optimized. Since free energy versus bond distance curves are steeper for deviations in shorter than in longer distances, the average distances will be greater for structures with greater deviations from ideal bonding distances. This effect corresponds to the well known thermal expansion. There the deviations from ideal bonding distances are dynamic, of course.

[^2]:    * The method employed was not sensitive enough to distinguish between the two.

[^3]:    * A direct proof and elaboration of this statement could be accomplished by least-squares and angles refinements as discussed by Shoemaker \& Shoemaker (1967), Meier \& Villiger (1969), and Baur (1971).

